

## Ellicott Dredge Laws

### DREDGING SYSTEMS AND THE BASIC DREDGE LAWS ©

Download the Basic Dredge Laws  
requires Acrobat Reader

Each dredge law provides you with a fundamental and convenient relationship between two or more of the factors which affect dredge production. By the judicious application of these laws, you will be able to understand the complex dredging cycle and to make the changes in design or operating procedure to maximize the output of a given dredge.

ABBREVIATIONS USED		
~	=	Varies as
$V_s$	=	Velocity in suction pipe
$d_s$	=	Diameter of suction pipe
$A_s$	=	Area of suction pipe
$h_v$	=	Velocity head
$h_E$	=	Entrance loss
$h_f$	=	Friction loss
$h_{sg}$	=	Head requirement for specific gravity over 1.0
$H$	=	Total dynamic head
D.D.	=	Digging depth
S.G. or sg	=	Specific gravity
$h_b$	=	Barometric head
$g$	=	Acceleration due to gravity
$h_s$	=	Suction head

- 1 - PRODUCTION VARIES AS FLOW X AVERAGE % SOLIDS.
- 2 - AVG. % SOLIDS = PEAK % SOLIDS X DREDGE EFFICIENCY.
- 3 - PEAK % SOLIDS VARIES AS  $V_s$ ; TYPE OF SOLIDS:
- 4 - MAXIMUM (SHORT LINE) PRODUCTION VARIES AS AREA OF SUCTION PIPE
- 5 - OPTIMUM  $V_s$  VARIES AS DIGGING DEPTH
- 6 - DISCHARGE LINE LENGTH VARIES AS PUMP HP
- 7 - PRODUCTION IS LIMITED BY
  - (1) Suction Conditions (Barometric Head)
  - (2) Pump HP Available (Discharge Head Requirement)
  - (3) Velocity (Conveying Capacity)

1 - PRODUCTION VARIES AS FLOW X AVERAGE % SOLIDS.

It is appropriate that the first dredge law deals with the economic purpose of a dredge, the production (i.e. excavation and transport) of solids. This law is obvious and generally accepted.

---

SKETCH NO. 1

PRODUCTION VARIES AS FLOW X AVE % SOLIDS

IN COUNTRIES USING THE ENGLISH SYSTEM, PRODUCTION IS NORMALLY IN UNITS OF YDS<sup>3</sup>/HR & FLOW IN G.P.M., WHILE % SOLIDS IS IN-SITU VOLUME INCLUDING VOIDS, NOT TRUE VOLUME. THE LAW IS TRUE REGARDLESS OF THE UNITS USED ALTHOUGH CONSTANTS MUST BE CHANGED WHERE UNITS ARE CHANGED. THE TRUE EQUATION IN ENGLISH UNITS IS

$$\text{YDS}^3/\text{HR} = \text{GPM} \times \text{AVE \% SOLIDS} \times .297$$

WHERE

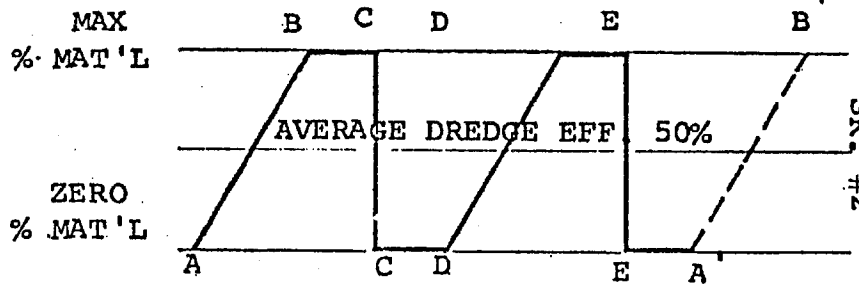
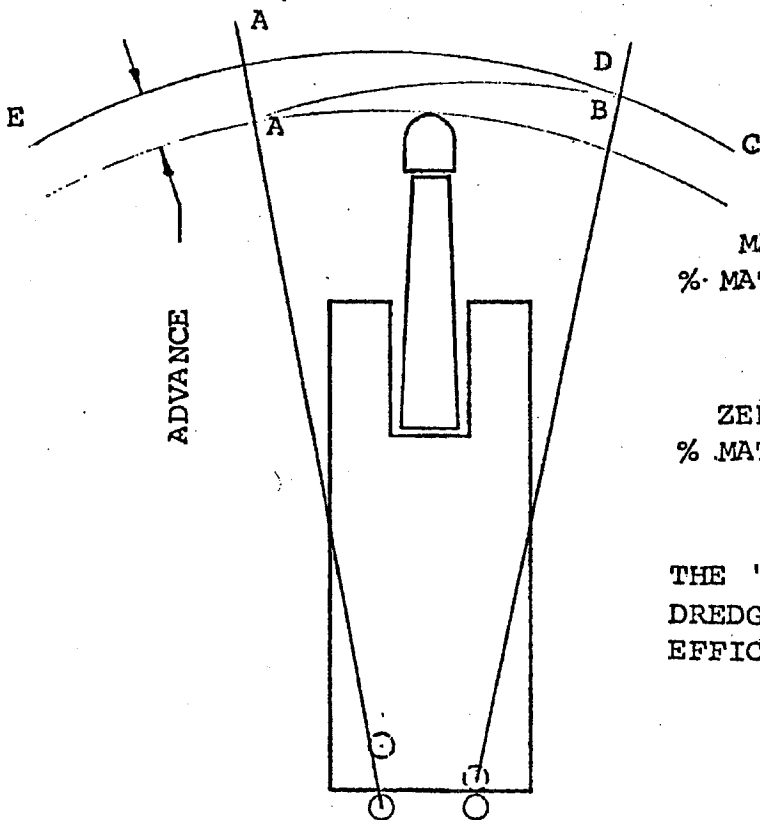
$$.297 = \frac{60 \text{ MIN.}/\text{HR.}}{7.48 \text{ GAL}/\text{FT}^3 \times 27 \text{ FT}^3/\text{YD}^3}$$

$$2 - \text{AVG. \% SOLIDS} = \text{PEAK \% SOLIDS} \times \text{DREDGE EFFICIENCY.}$$

The peak % solids is the maximum % solids the suction line can carry at any moment, and is limited by the cavitation point of the dredge pump. The dredge efficiency is the average % solids divided by the peak % solids, but since this is an abstract, mathematical expression, it can be simply explained as the actual production of the dredge compared with the production which would be realized if the maximum instantaneous rate were achieved continuously.

SKETCH NO. 2

$$\text{AVE \% SOLIDS} = \text{PEAK \% SOLIDS} \times \text{DREDGE EFF.}$$



THE "WALKING" (ADVANCING OPERATION) OF A DREDGE IS A MAJOR FACTOR AFFECTING DREDGE EFFICIENCY.

3 - PEAK % SOLIDS VARIES AS  $V_s$ ; TYPE OF SOLIDS:

It is apparent that low velocities will not carry high % solids since low velocities have low turbulence and would "drop out" or fail to transport the materials. It should be emphasized that the velocity which determines the dredge production is the suction line velocity, not the discharge line velocity.

The type of solids also affects the % solids transported at a given velocity. If the particle size is relatively large and dense, a greater turbulence is required to keep it in suspension. Empirical data is generally required here, although theoretical equations have been developed for homogeneous materials.

The most frequently overlooked factor affecting % solids is the diameter of the suction pipe. A brief analysis of any pipe line friction equation will disclose that at a given velocity, the friction (and therefore turbulence) decreases as the diameter increases. This decreased turbulence allows the transport of less material; therefore, to transport the same % as a smaller line, the velocity in a large line must be increased to obtain the same turbulence. The relationship is a function of the square root of the diameter.

---

SKETCH NO. 3

PEAK % SOLIDS VARIES AS (1)  $V_s$ ; (2) TYPE OF SOLIDS; (3)  $\frac{1}{\sqrt{d_s}}$

TURBULENCE IN THE CARRYING MEDIUM IS REQUIRED TO KEEP SOLIDS SUSPENDED.

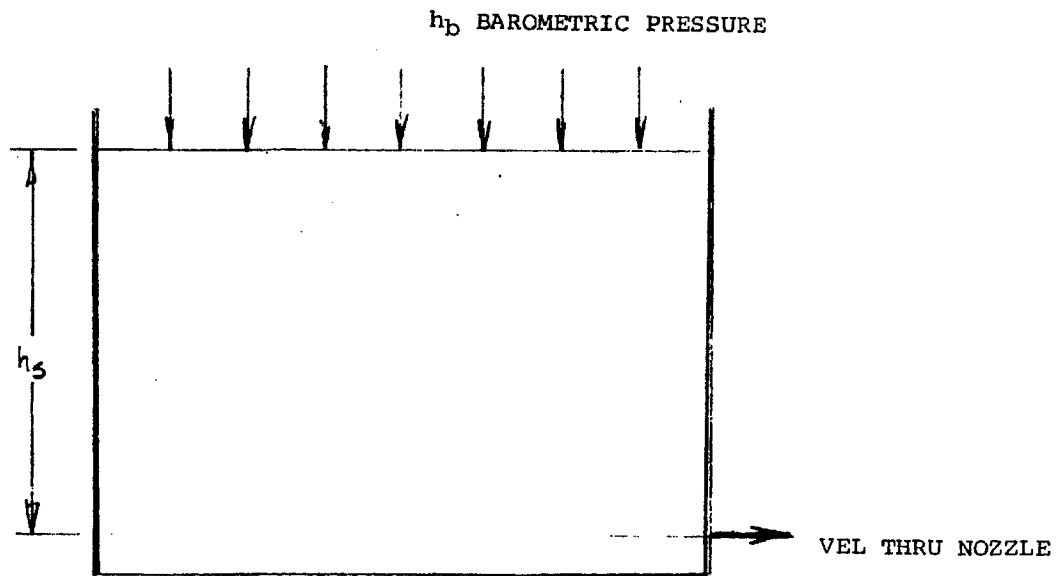
- (1) THE GREATER THE VELOCITY, THE GREATER THE TURBULENCE.
- (2) THE DENSER AND LARGER (UP TO A POINT) THE SOLIDS, THE GREATER THE TURBULENCE REQUIRED TO SUSPEND AND TRANSPORT THE SOLIDS.
- (3) THE LARGER THE PIPE, THE LOWER THE TURBULENCE AT A GIVEN VELOCITY.

4 - MAXIMUM (SHORT LINE) PRODUCTION VARIES AS AREA OF SUCTION PIPE

A dredge pump is a device that evacuates its casing; it cannot reach down the suction pipe to pick up the slurry. The only force available to push the slurry to a dredge pump mounted at water level is the barometric pressure. The design of the "Barometric Pump" is perhaps the most critical aspect of the dredge, for as all dredge men know, if the dredge pump is run faster than the suction line can deliver slurry, cavitation results.

An analysis of the basic hydraulic equation  $h = \frac{V^2}{2g}$  discloses that  $h$  varies as  $V^2$  and  $V$  varies as the square root of  $h$ . since the only  $h$  available to force slurry through the suction pipe is the barometric head (constant at sea level), the maximum velocity is a constant. It follows then that since Flow = Vel. (a constant) x Area, the Flow and Production vary as  $A_s$ .

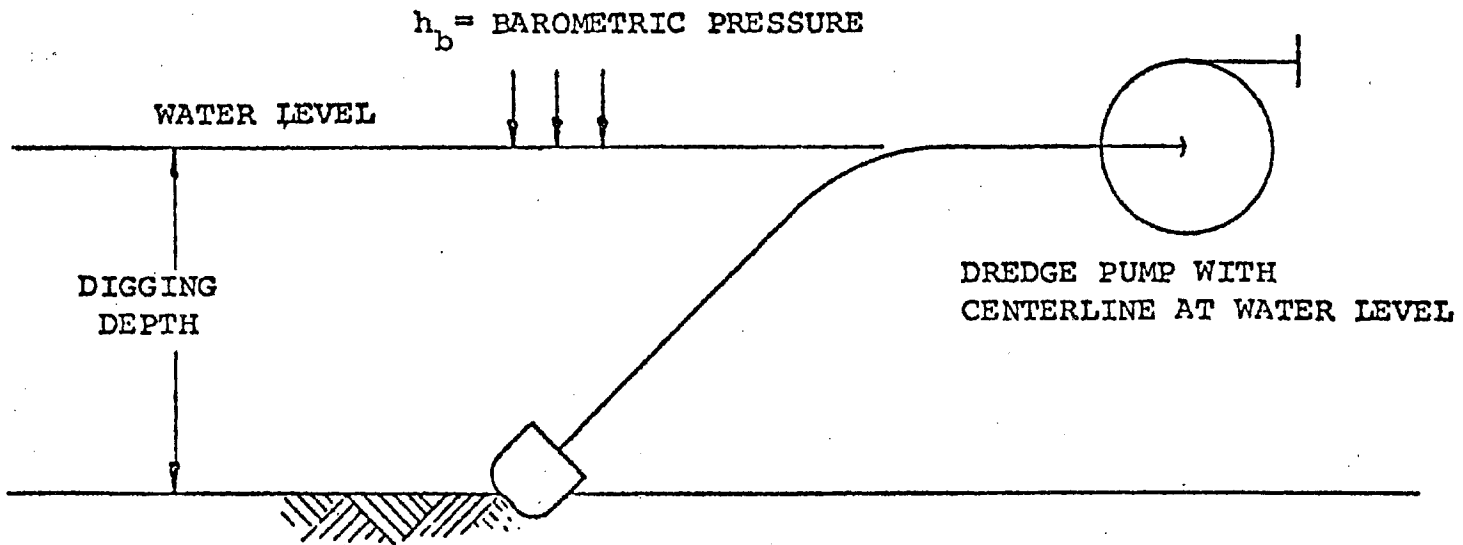
SKETCH NO. 4A



- $h_s = \frac{V^2}{2g}$  EQUATION EXPRESSING BASIC HEAD-VELOCITY RELATIONSHIP.
- $h_s \quad V^2$  CONSTANTS ELIMINATED; RELATIONSHIP UN-ALTERED.
- $V \quad \overline{h_s}$  TRANSPOSITION OF TERMS ONLY, AND ASSUMING DISCHARGE AGAINST BAROMETRIC PRESSURE.
- $V \quad \overline{h_s + h_b}$  ASSUMING DISCHARGE AGAINST ABSOLUTE ZERO.
- $V \quad \overline{h_b}$  ASSUMING DISCHARGE AGAINST ABSOLUTE ZERO AND  $h_s$  ELIMINATED

---

MAX. OR SHORT LINE PRODUCTION  $\sim A_s$



SINCE  $h$  IS BAROMETRIC PRESSURE AND A CONSTANT, MAX.  $V$  IS CONSTANT

SINCE  $\text{FLOW} = V \times A$ , THEN  $\text{FLOW} \sim A$

SINCE PRODUCTION VARIES AS FLOW (DREDGE LAW I), IT ALSO VARIES AS  $A$

---

5 - OPTIMUM  $V_s$  VARIES AS DIGGING DEPTH

By an analysis of the suction line losses,  $h_v$ ;  $h_e$ ;  $h_f$ ;  $h_{sg}$  it can be demonstrated that since the sum total of these must equal barometric head, regardless of digging depth, that it is necessary to trade off velocity head for specific gravity head as digging depth increases. A reduction in velocity head reduces velocity and requires a reduction in pump speed; therefore, GPM and pump speed must diminish to an optimum value as digging depth increases.

SKETCH NO. 5

OPTIMUM  $V_s$   $\sim$  DIGGING DEPTH

LOSS FACTOR	WATER	SLURRY	
	AT 16 FT/SEC	30' D.D. 1.5 S.G.	50' D.D. 1.36 S.G.
$h_v = \frac{V^2}{2g} \times S.G.$	4	6	5
$h_E = K \frac{V^2}{2g} \times S.G.*$	2	6	5
$h_F = K \frac{V^2}{2g} \times S.G.**$	1	3	2
$h_{SG} = D.D. (S.G. \text{ slurry} - S.G. \text{ water} )$	$\frac{0}{7'}$	$\frac{15}{30'}$	$\frac{18}{30'}$

BY REFERRING TO DREDGE LAW #1,  
 PRODUCTION  $\sim$  FLOW X AVE % SOLIDS,

IT BECOMES OBVIOUS THAT AT 50' DIGGING DEPTH BOTH FLOW & % SOLIDS HAVE DECREASED: THEREFORE AS D.D. INCREASES, PRODUCTION DECREASES IN AN EXPONENTIAL MANNER.

\* K FOR THESE CALCULATIONS IS ASSUMED TO BE .5 WHEN PUMPING WATER;  
 1.0 WHEN PUMPING SLURRY.

\*\* IN ORDER TO AVOID THE USE OF DECIMALS, THESE FRICTION FIGURES ARE QUITE ROUGH.

## 6 - DISCHARGE LINE LENGTH VARIES AS PUMP HP

An analysis of the HP equation shows that since GPM is a constant at a given digging depth, and since pump efficiency is a constant at a given GPM, that HP varies as head which, in turn, varies as discharge line length; therefore, HP determines not maximum output but rather how far it can be pumped. If it is desired to pump further, a booster must be added or the % solids reduced.

---

### SKETCH NO. 6

$$HP = \frac{GPM \times 8.34 \times S.G. \times H}{33000 \times EFF}$$

BY ELIMINATING ALL CONSTANTS AND IGNORING THE RELATIVELY SMALL SUCTION LINE LOSSES, WE GET

HP  $\sim$  H  $\sim$  LINE LENGTH

GPM SHOULD BE CONSTANT FOR ANY GIVEN DIGGING DEPTH.

AVERAGE S.G. IS A FUNCTION OF VELOCITY, AND, THEREFORE CONSTANT

EFF IS CONSTANT AT CONSTANT GPM.

7 - PRODUCTION IS LIMITED BY

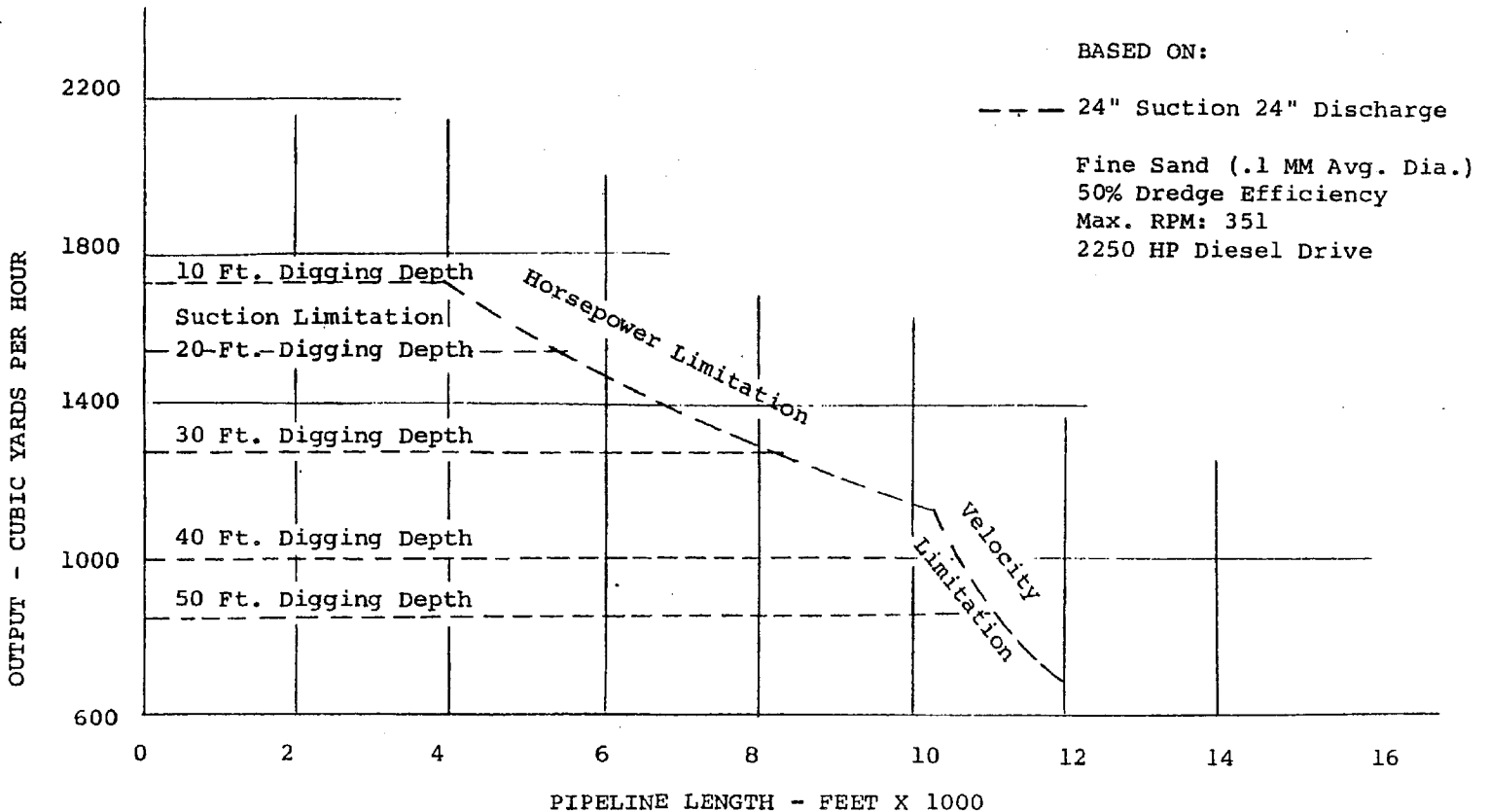
- (1) Suction Conditions (Barometric Head)
- (2) Pump HP Available (Discharge Head Requirement)
- (3) Velocity (Conveying Capacity)

The seventh law is a general statement of the first six laws. A typical production chart is attached which shows the effect of the limitations imposed by suction conditions (horizontal lines), the pump HP (sloping lines) and the velocity carrying capacity (curved asymptotic line).

SKETCH NO. 7A

- PRODUCTION IS LIMITED BY:
- 1. Suction Conditions
  - 2. Pump H.P. Available.
  - 3. Suction Velocity

CALCULATED OUTPUT CURVES

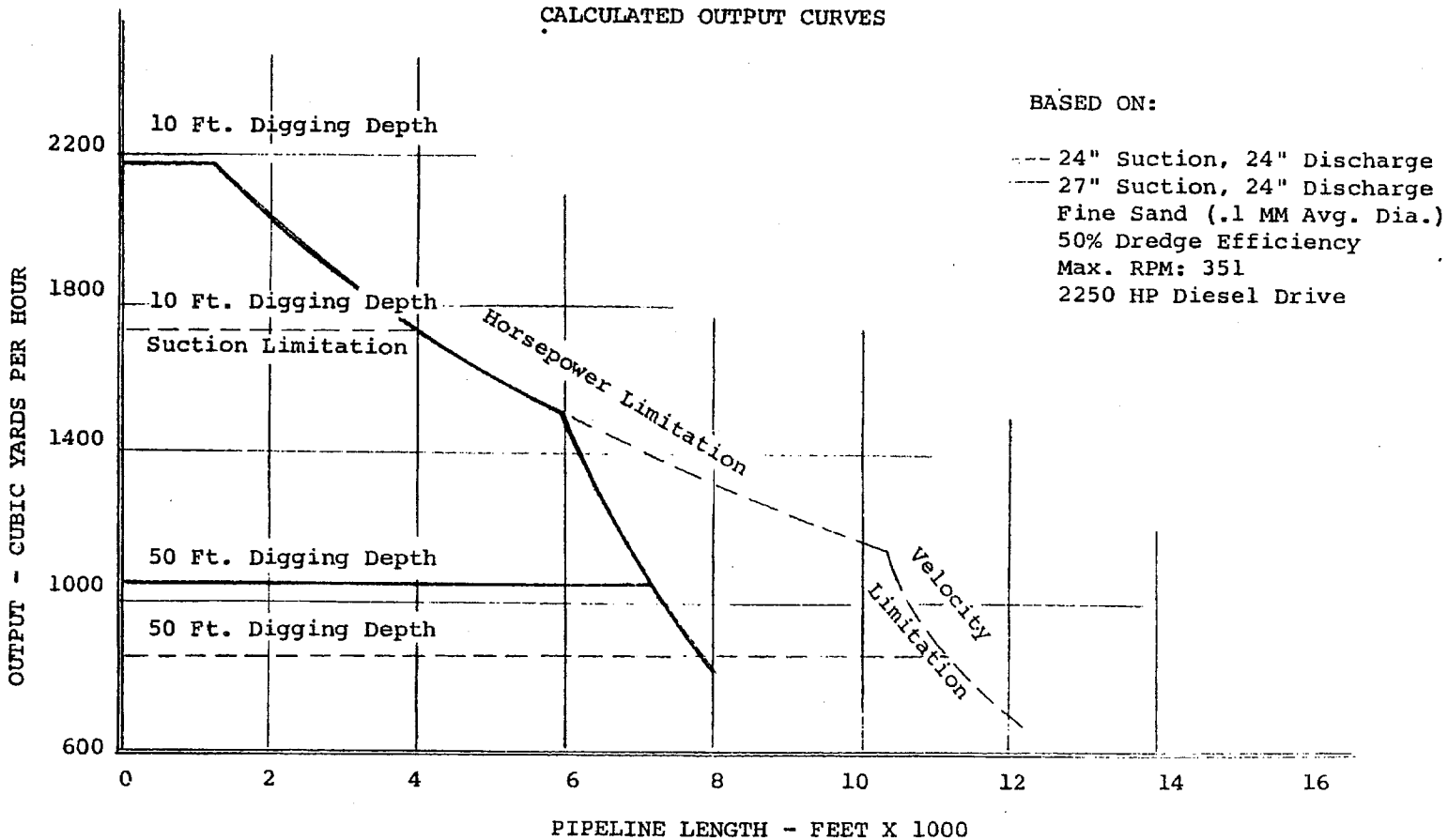


Now, we hope it is obvious to you after your exposure to the Dredge Laws, that there are ways to eliminate the restrictions on production as manifest in these production charts. First, let's look at the effect of increasing the suction size (Sketch No. 7B). You will see the short line production increases in proportion to the area of the suction line (Dredge Law #4) but now the HP is not available to pump it as far.

SKETCH NO. 7B

- PRODUCTION IS LIMITED BY:
- (1) Suction Conditions
  - (2) Pump HP Available
  - (3) Suction Velocity

CALCULATED OUTPUT CURVES

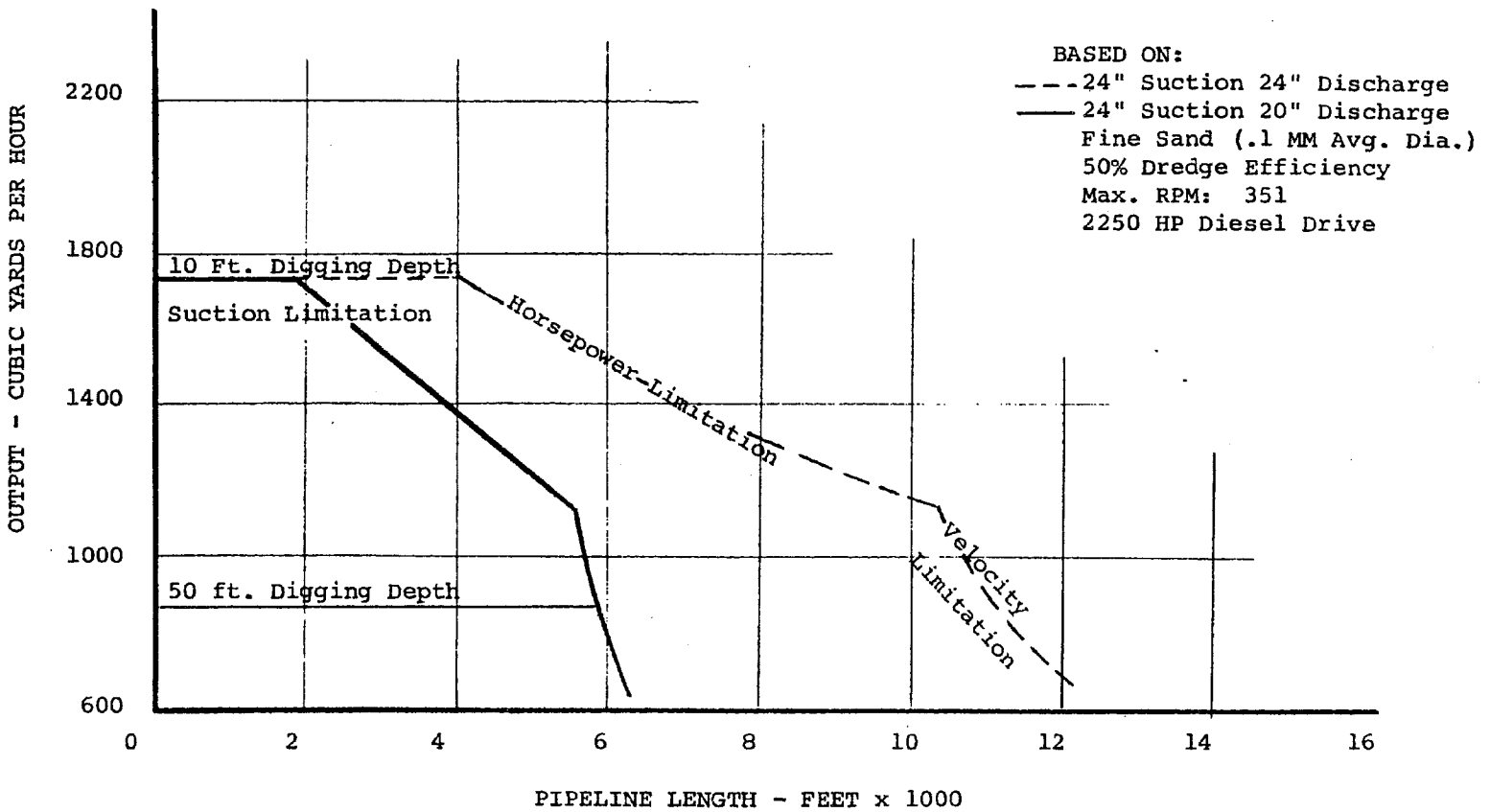


Next, let's use a 20" discharge line rather than a 24". The maximum production is still the same, but since  $h_f$  varies as  $d_d^{-4.85}$  (Hazen & Williams formula) it cannot be pumped as far.

SKETCH NO. 7C

- PRODUCTION IS LIMITED BY:
- (1) Suction Conditions
  - (2) Pump HP Available
  - (3) Suction Velocity

CALCULATED OUTPUT CURVES



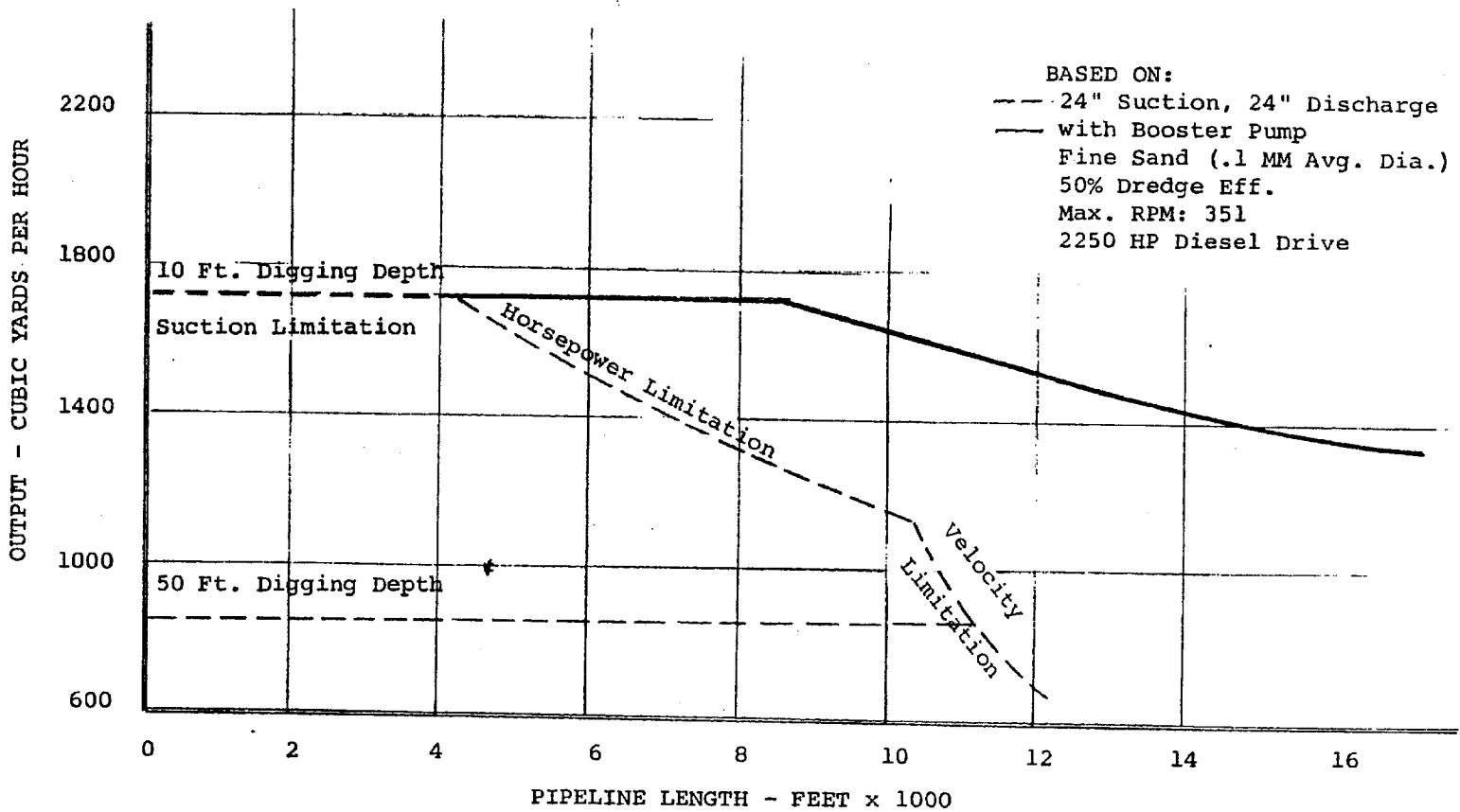
Suppose we add a booster pump (Sketch No. 7D). The maximum production remains the same (D.L. #4), but the pumping distance is essentially doubled since the HP is doubled (D.L. #6)

SKETCH NO. 7D

PRODUCTION IS LIMITED BY:

- (1) Suction Conditions
- (2) Pump HP Available
- (3) Suction Velocity

CALCULATED OUTPUT CURVES



Now, consider the addition of a pump on the ladder to attack the suction limitation. Note that not only is the 10' DD output increased, but the depth at 50' is more than doubled. If you need to dig to 100', the output would be quadrupled giving the output of an additional three dredges at 5% of the investment, and without the other three operating crews. Booster pumps can be added also, if needed.

SKETCH NO. 7E

- PRODUCTION IS LIMITED BY:
- (1) Suction Conditions
  - (2) Pump HP Available
  - (3) Suction Velocity

CALCULATED OUTPUT CURVES

